## Advanced Performance Management

Friday 6 June 2008


## Time allowed

Reading and planning: 15 minutes
Writing:
3 hours

This paper is divided into two sections:
Section A - BOTH questions are compulsory and MUST be attempted
Section B - TWO questions ONLY to be attempted

Do NOT open this paper until instructed by the supervisor.
During reading and planning time only the question paper may be annotated. You must NOT write in your answer booklet until instructed by the supervisor.
This question paper must not be removed from the examination hall.


## Section A - BOTH questions are compulsory and MUST be attempted

1 The Health and Fitness Group (HFG), which is privately owned, operates three centres in the country of Mayland. Each centre offers dietary plans and fitness programmes to clients under the supervision of dieticians and fitness trainers. Residential accommodation is also available at each centre. The centres are located in the towns of Ayetown, Beetown and Ceetown.

The following information is available:
(1) Summary financial data for HFG in respect of the year ended 31 May 2008.

|  | Ayetown \$000 | $\begin{aligned} & \text { Beetown } \\ & \$ 000 \end{aligned}$ | $\begin{aligned} & \text { Ceetown } \\ & \$ 000 \end{aligned}$ | $\begin{aligned} & \text { Total } \\ & \$ 000 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
| Revenue: |  |  |  |  |
| Fees received | 1,800 | 2,100 | 4,500 | 8,400 |
| Variable costs | (468) | (567) | $(1,395)$ | $(2,430)$ |
| Contribution | 1,332 | 1,533 | 3,105 | 5,970 |
| Fixed costs | (936) | $(1,092)$ | $(2,402)$ | $(4,430)$ |
| Operating profit | 396 | 441 | 703 | 1,540 |

Interest costs on long-term debt at 10\%
Profit before tax $\frac{(180)}{1,360}$

| Income tax expense |  |
| :--- | :--- |
| Profit for the year | $\frac{1408)}{952}$ |

Average book values for 2008:

| Assets |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Non-current assets | 1,000 | 2,500 | 3,300 | 6,800 |
| Current assets | 800 | 900 | 1,000 | 2,700 |
| Total assets | 1,800 | 3,400 | 4,300 | 9,500 |
| Equity and liabilities: |  |  |  |  |
| Share capital |  |  |  | 2,500 |
| Retained earnings |  |  |  | 4,400 |
| Total equity |  |  |  | 6,900 |
| Non-current liabilities |  |  |  |  |
| Long-term borrowings |  |  |  | 1,800 |
| Total non-current liabilities |  |  |  | 1,800 |
| Current liabilities | 80 | 240 | 480 | 800 |
| Total current liabilities | 80 | 240 | 480 | 800 |
| Total liabilities |  |  |  | 2,600 |
| Total equity and liabilities |  |  |  | 9,500 |

(2) HFG defines Residual Income (RI) for each centre as operating profit minus a required rate of return of $12 \%$ of the total assets of each centre.
(3) At present HFG does not allocate the long-term borrowings of the group to the three separate centres.
(4) Each centre faces similar risks.
(5) Tax is payable at a rate of $30 \%$.
(6) The market value of the equity capital of HFG is $\$ 9$ million. The cost of equity of HFG is $15 \%$.
(7) The market value of the long-term borrowings of HFG is equal to the book value.
(8) The directors are concerned about the return on investment (ROI) generated by the Beetown centre and they are considering using sensitivity analysis in order to show how a target ROI of $20 \%$ might be achieved.
(9) The marketing director stated at a recent board meeting that 'The Group's success depends on the quality of service provided to our clients. In my opinion, we need only to concern ourselves with the number of complaints received from clients during each period as this is the most important performance measure for our business. The number of complaints received from clients is a perfect performance measure. As long as the number of complaints received from clients is not increasing from period to period, then we can be confident about our future prospects'.

## Required:

(a) The directors of HFG have asked you, as management accountant, to prepare a report providing them with explanations as to the following:
(i) Which of the three centres is the most 'successful'? Your report should include a commentary on return on investment (ROI), residual income (RI), and economic value added (EVA) as measures of financial performance. Detailed calculations regarding each of these three measures must be included as part of your report;

Note: a maximum of seven marks is available for detailed calculations.
(14 marks)
(ii) The percentage change in revenue, total costs and net assets during the year ended 31 May 2008 that would have been required in order to have achieved a target ROI of $20 \%$ by the Beetown centre. Your answer should consider each of these three variables in isolation. State any assumptions that you make.
(iii) Whether or not you agree with the statement of the marketing director in note (9) above.

Professional marks for appropriateness of format, style and structure of the report.
(b) The Superior Fitness Co (SFC), which is well established in Mayland, operates nine centres. Each of SFC's centres is similar in size to those of HFG. SFC also provides dietary plans and fitness programmes to its clients. The directors of HFG have decided that they wish to benchmark the performance of HFG with that of SFC.

## Required:

Discuss the problems that the directors of HFG might experience in their wish to benchmark the performance of HFG with the performance of SFC, and recommend how such problems might be successfully addressed.
(7 marks)
(36 marks)

2 The Rubber Group (TRG) manufactures and sells a number of rubber-based products. Its strategic focus is channelled through profit centres which sell products transferred from production divisions that are operated as cost centres. The profit centres are the primary value-adding part of the business, where commercial profit centre managers are responsible for the generation of a contribution margin sufficient to earn the target return of TRG. The target return is calculated after allowing for the sum of the agreed budgeted cost of production at production divisions, plus the cost of marketing, selling and distribution costs and central services costs.

The Bettamould Division is part of TRG and manufactures moulded products that it transfers to profit centres at an agreed cost per tonne. The agreed cost per tonne is set following discussion between management of the Bettamould Division and senior management of TRG.

The following information relates to the agreed budget for the Bettamould Division for the year ending 30 June 2009:
(1) The budgeted output of moulded products to be transferred to profit centres is 100,000 tonnes. The budgeted transfer cost has been agreed on a two-part basis as follows:
(i) A standard variable cost of $\$ 200$ per tonne of moulded products;
(ii) A lump sum annual charge of $\$ 50,000,000$ in respect of fixed costs, which is charged to profit centres, at $\$ 500$ per tonne of moulded products.
(2) Budgeted standard variable costs (as quoted in 1 above) have been set after incorporating each of the following:
(i) A provision in respect of processing losses amounting to $15 \%$ of material inputs. Materials are sourced on a JIT basis from chosen suppliers who have been used for some years. It is felt that the $15 \%$ level of losses is necessary because the ageing of the machinery will lead to a reduction in the efficiency of output levels.
(ii) A provision in respect of machine idle time amounting to $5 \%$. This is incorporated into variable machine costs. The idle time allowance is held at the $5 \%$ level partly through elements of 'real-time' maintenance undertaken by the machine operating teams as part of their job specification.
(3) Quality checks are carried out on a daily basis on $25 \%$ of throughput tonnes of moulded products.
(4) All employees and management have contracts based on fixed annual salary agreements. In addition, a bonus of $5 \%$ of salary is payable as long as the budgeted output of 100,000 tonnes has been achieved;
(5) Additional information relating to the points in (2) above (but NOT included in the budget for the year ending 30 June 2009) is as follows:
(i) There is evidence that materials of an equivalent specification could be sourced for $40 \%$ of the annual requirement at the Bettamould Division, from another division within TRG which has spare capacity.
(ii) There is evidence that a move to machine maintenance being outsourced from a specialist company could help reduce machine idle time and hence allow the possibility of annual output in excess of 100,000 tonnes of moulded products.
(iii) It is thought that the current level of quality checks (25\% of throughput on a daily basis) is vital, although current evidence shows that some competitor companies are able to achieve consistent acceptable quality with a quality check level of only $10 \%$ of throughput on a daily basis.
The directors of TRG have decided to investigate claims relating to the use of budgeting within organisations which have featured in recent literature. A summary of relevant points from the literature is contained in the following statement:
'The use of budgets as part of a 'performance contract' between an organisation and its managers may be seen as a practice that causes management action which might lead to the following problems:
(a) Meeting only the lowest targets
(b) Using more resources than necessary
(c) Making the bonus - whatever it takes
(d) Competing against other divisions, business units and departments
(e) Ensuring that what is in the budget is spent
(f) Providing inaccurate forecasts
(g) Meeting the target, but not beating it
(h) Avoiding risks.'

Required:
(a) Explain the nature of any SIX of the eight problems listed above relating to the use of budgeting;
(b) Illustrate EACH of the six problems chosen in (a) using the data from the Bettamould division/TRG scenario; and
(c) Suggest ways in which each of the six problems chosen in (a) above may be overcome.

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Question 3 begins on page 7.

## Section B - TWO questions ONLY to be attempted

3 The Global Hotel Group (GHG) operates hotels in most of the developed countries throughout the world. The directors of GHG are committed to a policy of achieving 'growth' in terms of geographical coverage and are now considering building and operating another hotel in Tomorrowland. Tomorrowland is a developing country which is situated 3,000 kilometres from the country in which GHG's nearest hotel is located.

The managing director of GHG recently attended a seminar on 'the use of strategic and economic information in planning organisational performance'.

He has called a board meeting to discuss the strategic and economic factors which should be considered before a decision is made to build the hotel in Tomorrowland.

## Required:

(a) Discuss the strategic and economic factors which should be considered before a decision is made to build the hotel.
(14 marks)
(b) GHG has always used local labour to build and subsequently operate hotels. The directors of GHG are again considering employing a local workforce not only to build the hotel but also to operate it on a daily basis.

## Required:

Explain TWO ways in which the possibility of cultural differences might impact on the performance of a local workforce in building and operating a hotel in Tomorrowland.

4 The Childrens Toy Company (CTC) manufactures electrically-operated toy versions of animals. The activities of CTC are confined to the country of Stableland, which has a zero-inflation economy. The government of Stableland has granted tax-exempt status to CTC since it provides goods or services exclusively for children. However, no tax allowances are available on investments made by CTC.

CTC has a total production capacity of 400,000 units which cannot be exceeded. The products to be manufactured together with forecast sales volumes are as follows:

| Product | Forecast sales units ('000) |  |  |  |
| :--- | :---: | :---: | :---: | ---: |
|  | 2008 | 2009 | 2010 | 2011 |
| Bruno the Bear | 180 | 120 | 100 | 60 |
| Kong the Ape | 150 | 48 | 24 | 0 |
| Leo the Lion | 60 | 72 | 76 | 30 |

Other relevant information relating to the products is as follows:

1. Selling prices per unit and contribution to sales ratios (\%) for 2008 and 2009:

| Selling price | Contribution to |
| :--- | :--- |
| per unit (\$) | sales ratio (\%) |

Product:

| Bruno | 40 | 70 |
| :--- | :--- | :--- |
| Kong | 50 | 65 |

2. Product-specific fixed overheads:

| Year | 2008 | 2009 |
| :--- | ---: | ---: |
|  | $\$ 000$ | $\$ 000$ |
| Bruno | 3,800 | 2,400 |
| Kong | 2,400 | 1,340 |
| Leo | 2,040 | 2,100 |

3. The company's other fixed overheads are estimated at $\$ 1.65$ million per annum.

## Required:

(a) (i) Prepare a statement of product profitability for each of years 2008 and 2009 which also shows the net profit or loss of CTC.
(ii) Comment on the figures in the statement prepared in (a)(i) above.
(b) The marketing director of CTC has suggested the introduction of a new toy 'Nellie the Elephant' for which the following estimated information is available:

1. Sales volumes and selling prices per unit

| Year ending, 31 May | 2009 | 2010 | 2011 |
| :--- | :---: | :---: | :---: |
| Sales units (000) | 80 | 180 | 100 |
| Selling price per unit (\$) | 50 | 50 | 50 |

2. Nellie will generate a contribution to sales ratio of $50 \%$ throughout the three year period.
3. Product specific fixed overheads during the year ending 31 May 2009 are estimated to be $\$ 1 \cdot 6$ million. It is anticipated that these fixed overheads would decrease by $10 \%$ per annum during each of the years ending 31 May 2010 and 31 May 2011.
4. Capital investment amounting to $\$ 3.9$ million would be required in June 2008. The investment would have no residual value at 31 May 2011.
5. Additional working capital of $\$ 500,000$ would be required in June 2008. A further $\$ 200,000$ would be required on 31 May 2009. These amounts would be recovered in full at the end of the three year period.
6. The cost of capital is expected to be $12 \%$ per annum.

Assume all cash flows (other than where stated) arise at the end of the year.

## Required:

(i) Determine whether the new product is viable purely on financial grounds.
(ii) Calculate the minimum target contribution to sales ratio (\%) at which 'Nellie the Elephant' will be financially viable, assuming that all other data remain unchanged.
(iii) Identify and discuss an alternative strategy that may assist in improving the performance of CTC with effect from 1 May 2009 (where only the products in (a) and (b) above are available for manufacture).

5 Telecoms At Work (TAW) manufactures and markets office communications systems. During the year ended 31 May 2008 TAW made an operating profit of $\$ 30$ million on sales of $\$ 360$ million. However, the directors are concerned that products do not conform to the required level of quality and TAW is therefore not fulfilling its full potential in terms of turnover and profits achieved.

The following information is available in respect of the year ended 31 May 2008:
(1) Production data:

Units manufactured and sold 18,000
Units requiring rework 2,100
Units requiring warranty repair service $\quad 2,700$
Design engineering hours 48,000
Process engineering hours 54,000
Inspection hours (manufacturing) 288,000
(2) Cost data:

Design engineering per hour 96
Process engineering per hour 70
Inspection per hour (manufacturing) 50
Rework per communication system reworked (manufacturing) 4,800
Customer support per repaired unit (marketing) 240
Transportation costs per repaired unit (distribution) 280
Warranty repairs per repaired unit (customer service) 4,600
(3) Staff training costs amounted to $\$ 180,000$ and additional product testing costs of $\$ 72,000$.
(4) The marketing director has estimated that sales of 1,800 units were lost as a result of public knowledge of poor quality at TAW. The average contribution per communication system is estimated at \$7,200.

## Required:

(a) Prepare a cost analysis which shows actual prevention costs, appraisal costs, internal failure costs, and external failure costs for the year ended 31 May 2008. Your statement should show each cost heading as a $\%$ of turnover and clearly show the total cost of quality. Comment briefly on the inclusion of opportunity costs in such an analysis.
(11 marks)
(b) A detailed analysis has revealed that the casings in which the communications systems are housed are often subject to mishandling in transit to TAW's manufacturing premises. The directors are considering two alternative solutions proposed by the design engineering team which are aimed at reducing the quality problems that are currently being experienced. These are as follows:

Option 1 - Increase the number of immediate physical inspections of the casings when they are received from the supplier. This will require an additional 10,000 inspection hours.

Option 2 - Redesign and strengthen the casings and the containers used to transport them to better withstand mishandling during transportation. Redesign will require an additional 2,000 hours of design engineering and an additional 5,000 hours of process engineering.

Internal failure costs of rework for each reworked communication system are as follows:

## \$

| Variable costs | (including direct materials, direct labour rework and supplies) | 1,920 |
| :--- | :--- | :--- |
| Allocated fixed costs | (equipment, space and allocated overhead) | 2,880 |
| Total costs (as per note 2 on cost data) | 4,800 |  |

The directors of TAW believe that, even if it is able to achieve improvements in quality, it will be unable to save any of the fixed costs of internal and external failure.
If TAW chooses to inspect the casings more carefully, it expects to eliminate re-work on 720 communication systems whereas if it redesigns the casings it expects to eliminate rework on 960 communication systems.

If incoming casings are inspected more carefully, TAW estimates that 600 fewer communication systems will require warranty repair and that it will be able to sell an additional 300 communication systems. If the casing is redesigned, the directors estimate that 840 fewer communication systems will require warranty repair and that an additional 360 communication systems will be sold.

External failure costs of repair for each repaired communication system are as follows:

|  | Variable costs | Fixed costs | Total costs |
| :--- | :---: | :---: | :---: |
|  | $\$$ | $\$$ | $\$$ |
| Customer support costs | 96 | 144 | 240 |
| Transportation costs | 210 | 70 | 280 |
| Warranty repair costs | 1,700 | 2,900 | 4,600 |

## Required:

Prepare an estimate of the financial consequences of each option and advise the directors of TAW which option should be chosen.

## Present Value Table

Present value of 1 i.e. $(1+r)^{-n}$
Where $\quad r=$ discount rate
$\mathrm{n}=$ number of periods until payment

Discount rate (r)
Periods

| (n) | $1 \%$ | $2 \%$ | $3 \%$ | $4 \%$ | $5 \%$ | $6 \%$ | $7 \%$ | $8 \%$ | $9 \%$ | $10 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 0.980 | 0.961 | 0.943 | 0.925 | 0.907 | 0.890 | 0.873 | 0.857 | 0.842 | 0.826 | 2 |
| 3 | 0.971 | 0.942 | 0.915 | 0.889 | 0.864 | 0.840 | 0.816 | 0.794 | 0.772 | 0.751 | 3 |
| 4 | 0.961 | 0.924 | 0.888 | 0.855 | 0.823 | 0.792 | 0.763 | 0.735 | 0.708 | 0.683 | 4 |
| 5 | 0.951 | 0.906 | 0.863 | 0.822 | 0.784 | 0.747 | 0.713 | 0.681 | 0.650 | 0.621 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.942 | 0.888 | 0.837 | 0.790 | 0.746 | 0.705 | 0.666 | 0.630 | 0.596 | 0.564 | 6 |
| 7 | 0.933 | 0.871 | 0.813 | 0.760 | 0.711 | 0.665 | 0.623 | 0.583 | 0.547 | 0.513 | 7 |
| 8 | 0.923 | 0.853 | 0.789 | 0.731 | 0.677 | 0.627 | 0.582 | 0.540 | 0.502 | 0.467 | 8 |
| 9 | 0.914 | 0.837 | 0.766 | 0.703 | 0.645 | 0.592 | 0.544 | 0.500 | 0.460 | 0.424 | 9 |
| 10 | 0.905 | 0.820 | 0.744 | 0.676 | 0.614 | 0.558 | 0.508 | 0.463 | 0.422 | 0.386 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.896 | 0.804 | 0.722 | 0.650 | 0.585 | 0.527 | 0.475 | 0.429 | 0.388 | 0.350 | 11 |
| 12 | 0.887 | 0.788 | 0.701 | 0.625 | 0.557 | 0.497 | 0.444 | 0.397 | 0.356 | 0.319 | 12 |
| 13 | 0.879 | 0.773 | 0.681 | 0.601 | 0.530 | 0.469 | 0.415 | 0.368 | 0.326 | 0.290 | 13 |
| 14 | 0.870 | 0.758 | 0.661 | 0.577 | 0.505 | 0.442 | 0.388 | 0.340 | 0.299 | 0.263 | 14 |
| 15 | 0.861 | 0.743 | 0.642 | 0.555 | 0.481 | 0.417 | 0.362 | 0.315 | 0.275 | 0.239 | 15 |


| (n) | $11 \%$ | $12 \%$ | $13 \%$ | $14 \%$ | $15 \%$ | $16 \%$ | $17 \%$ | $18 \%$ | $19 \%$ | $20 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 0.812 | 0.797 | 0.783 | 0.769 | 0.756 | 0.743 | 0.731 | 0.718 | 0.706 | 0.694 | 2 |
| 3 | 0.731 | 0.712 | 0.693 | 0.675 | 0.658 | 0.641 | 0.624 | 0.609 | 0.593 | 0.579 | 3 |
| 4 | 0.659 | 0.636 | 0.613 | 0.592 | 0.572 | 0.552 | 0.534 | 0.516 | 0.499 | 0.482 | 4 |
| 5 | 0.593 | 0.567 | 0.543 | 0.519 | 0.497 | 0.476 | 0.456 | 0.437 | 0.419 | 0.402 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.535 | 0.507 | 0.480 | 0.456 | 0.432 | 0.410 | 0.390 | 0.370 | 0.352 | 0.335 | 6 |
| 7 | 0.482 | 0.452 | 0.425 | 0.400 | 0.376 | 0.354 | 0.333 | 0.314 | 0.296 | 0.279 | 7 |
| 8 | 0.434 | 0.404 | 0.376 | 0.351 | 0.327 | 0.305 | 0.285 | 0.266 | 0.249 | 0.233 | 8 |
| 9 | 0.391 | 0.361 | 0.333 | 0.308 | 0.284 | 0.263 | 0.243 | 0.225 | 0.209 | 0.194 | 9 |
| 10 | 0.352 | 0.322 | 0.295 | 0.270 | 0.247 | 0.227 | 0.208 | 0.191 | 0.176 | 0.162 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.317 | 0.287 | 0.261 | 0.237 | 0.215 | 0.195 | 0.178 | 0.162 | 0.148 | 0.135 | 11 |
| 12 | 0.286 | 0.257 | 0.231 | 0.208 | 0.187 | 0.168 | 0.152 | 0.137 | 0.124 | 0.112 | 12 |
| 13 | 0.258 | 0.229 | 0.204 | 0.182 | 0.163 | 0.145 | 0.130 | 0.116 | 0.104 | 0.093 | 13 |
| 14 | 0.232 | 0.205 | 0.181 | 0.160 | 0.141 | 0.125 | 0.111 | 0.099 | 0.088 | 0.078 | 14 |
| 15 | 0.209 | 0.183 | 0.160 | 0.140 | 0.123 | 0.108 | 0.095 | 0.084 | 0.074 | 0.065 | 15 |

## Annuity Table

Present value of an annuity of 1 i.e. $\frac{1-(1+r)^{-n}}{r}$

$$
\text { Where } \quad \begin{aligned}
r & =\text { discount rate } \\
n & =\text { number of periods }
\end{aligned}
$$

Discount rate (r)
Periods

| (n) | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 1.970 | 1.942 | 1.913 | 1.886 | 1.859 | 1.833 | 1.808 | 1.783 | 1.759 | 1.736 | 2 |
| 3 | 2.941 | 2.884 | 2.829 | $2 \cdot 775$ | $2 \cdot 723$ | $2 \cdot 673$ | $2 \cdot 624$ | 2.577 | 2.531 | 2.487 | 3 |
| 4 | 3.902 | 3.808 | $3 \cdot 717$ | 3.630 | 3.546 | $3 \cdot 465$ | $3 \cdot 387$ | $3 \cdot 312$ | 3.240 | $3 \cdot 170$ | 4 |
| 5 | 4.853 | $4 \cdot 713$ | $4 \cdot 580$ | 4.452 | $4 \cdot 329$ | $4 \cdot 212$ | 4.100 | 3.993 | $3 \cdot 890$ | $3 \cdot 791$ | 5 |
| 6 | $5 \cdot 795$ | $5 \cdot 601$ | $5 \cdot 417$ | $5 \cdot 242$ | 5.076 | 4.917 | $4 \cdot 767$ | $4 \cdot 623$ | $4 \cdot 486$ | 4.355 | 6 |
| 7 | 6.728 | $6 \cdot 472$ | 6.230 | 6.002 | $5 \cdot 786$ | $5 \cdot 582$ | $5 \cdot 389$ | $5 \cdot 206$ | 5.033 | 4.868 | 7 |
| 8 | 7.652 | 7.325 | 7.020 | 6.733 | 6.463 | 6.210 | 5.971 | $5 \cdot 747$ | 5.535 | $5 \cdot 335$ | 8 |
| 9 | 8.566 | $8 \cdot 162$ | $7 \cdot 786$ | 7.435 | $7 \cdot 108$ | 6.802 | 6.515 | $6 \cdot 247$ | 5.995 | $5 \cdot 759$ | 9 |
| 10 | 9.471 | 8.983 | $8 \cdot 530$ | $8 \cdot 111$ | $7 \cdot 722$ | $7 \cdot 360$ | $7 \cdot 024$ | $6 \cdot 710$ | $6 \cdot 418$ | $6 \cdot 145$ | 10 |
| 11 | $10 \cdot 37$ | 9.787 | $9 \cdot 253$ | $8 \cdot 760$ | $8 \cdot 306$ | 7.887 | 7.499 | $7 \cdot 139$ | $6 \cdot 805$ | $6 \cdot 495$ | 11 |
| 12 | $11 \cdot 26$ | $10 \cdot 58$ | 9.954 | 9.385 | 8.863 | 8.384 | 7.943 | 7.536 | $7 \cdot 161$ | 6.814 | 12 |
| 13 | $12 \cdot 13$ | 11.35 | $10 \cdot 63$ | 9.986 | $9 \cdot 394$ | 8.853 | 8.358 | 7.904 | $7 \cdot 487$ | $7 \cdot 103$ | 13 |
| 14 | 13.00 | $12 \cdot 11$ | 11.30 | $10 \cdot 56$ | 9.899 | 9.295 | $8 \cdot 745$ | 8.244 | $7 \cdot 786$ | $7 \cdot 367$ | 14 |
| 15 | 13.87 | $12 \cdot 85$ | 11.94 | $11 \cdot 12$ | $10 \cdot 38$ | $9 \cdot 712$ | $9 \cdot 108$ | 8.559 | 8.061 | $7 \cdot 606$ | 15 |
| ( n ) | 11\% | 12\% | 13\% | 14\% | 15\% | 16\% | 17\% | 18\% | 19\% | 20\% |  |
| 1 | 0.901 | 0.893 | $0 \cdot 885$ | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 1.713 | 1.690 | 1.668 | 1.647 | 1.626 | 1.605 | 1.585 | 1.566 | 1.547 | 1.528 | 2 |
| 3 | $2 \cdot 444$ | 2.402 | $2 \cdot 361$ | $2 \cdot 322$ | $2 \cdot 283$ | $2 \cdot 246$ | $2 \cdot 210$ | $2 \cdot 174$ | $2 \cdot 140$ | $2 \cdot 106$ | 3 |
| 4 | $3 \cdot 102$ | 3.037 | $2 \cdot 974$ | $2 \cdot 914$ | $2 \cdot 855$ | $2 \cdot 798$ | $2 \cdot 743$ | $2 \cdot 690$ | $2 \cdot 639$ | 2.589 | 4 |
| 5 | 3.696 | 3.605 | 3.517 | 3.433 | 3.352 | 3.274 | $3 \cdot 199$ | $3 \cdot 127$ | 3.058 | 2.991 | 5 |
| 6 | $4 \cdot 231$ | $4 \cdot 111$ | 3.998 | 3.889 | $3 \cdot 784$ | 3.685 | 3.589 | 3.498 | 3.410 | 3.326 | 6 |
| 7 | $4 \cdot 712$ | 4.564 | $4 \cdot 423$ | 4.288 | $4 \cdot 160$ | 4.039 | $3 \cdot 922$ | 3.812 | 3.706 | $3 \cdot 605$ | 7 |
| 8 | 5.146 | $4 \cdot 968$ | $4 \cdot 799$ | 4.639 | 4.487 | 4.344 | $4 \cdot 207$ | 4.078 | 3.954 | 3.837 | 8 |
| 9 | 5.537 | $5 \cdot 328$ | 5.132 | 4.946 | $4 \cdot 772$ | 4.607 | $4 \cdot 451$ | 4.303 | $4 \cdot 163$ | 4.031 | 9 |
| 10 | $5 \cdot 889$ | $5 \cdot 650$ | $5 \cdot 426$ | $5 \cdot 216$ | 5.019 | $4 \cdot 833$ | $4 \cdot 659$ | 4.494 | $4 \cdot 339$ | 4.192 | 10 |
| 11 | $6 \cdot 207$ | 5.938 | $5 \cdot 687$ | $5 \cdot 453$ | $5 \cdot 234$ | 5.029 | 4.836 | 4.656 | $4 \cdot 486$ | 4.327 | 11 |
| 12 | 6.492 | $6 \cdot 194$ | 5.918 | 5.660 | $5 \cdot 421$ | 5.197 | 4.988 | $4 \cdot 793$ | $4 \cdot 611$ | 4.439 | 12 |
| 13 | 6.750 | $6 \cdot 424$ | $6 \cdot 122$ | $5 \cdot 842$ | 5.583 | $5 \cdot 342$ | $5 \cdot 118$ | 4.910 | $4 \cdot 715$ | 4.533 | 13 |
| 14 | 6.982 | $6 \cdot 628$ | $6 \cdot 302$ | 6.002 | $5 \cdot 724$ | $5 \cdot 468$ | $5 \cdot 229$ | 5.008 | 4.802 | 4.611 | 14 |
| 15 | $7 \cdot 191$ | $6 \cdot 811$ | $6 \cdot 462$ | $6 \cdot 142$ | $5 \cdot 847$ | $5 \cdot 575$ | $5 \cdot 324$ | 5.092 | $4 \cdot 876$ | $4 \cdot 675$ | 15 |

## End of Question Paper

