## Strategic Professional - Options

## Advanced Financial Management (AFM)

## March/June 2019 - Sample Questions

##  <br> AFM ACCA

Time allowed: 3 hours 15 minutes
This question paper is divided into two sections:
Section A - This ONE question is compulsory and MUST be attempted
Section B - BOTH questions are compulsory and MUST be attempted
Formulae and tables are on pages 8-12.
Do NOT open this question paper until instructed by the supervisor.

This question paper must not be removed from the examination hall.


## Think Ahead <br> ACCA

The Association of Chartered Certified

## Section A - This ONE question is compulsory and MUST be attempted

1 Talam Co, a listed company, aims to manufacture innovative engineering products which are environmentally friendly and sustainable. These products have been highly marketable because of their affordability. Talam Co's mission statement also states its desire to operate to the highest ethical standards. These commitments have meant that Talam Co has a very high reputation and a high share price compared to its competitors.

Talam Co is considering a new project, the Uwa Project, to manufacture drones for use in the agricultural industry, which are at least $50 \%$ biodegradable, at competitive prices. The drones will enable farmers to increase crop yields and reduce crop damage. Manufacture of drones is a new business area for Talam Co. The project is expected to last for four years.

Talam Co will also work on the Jigu Project (a follow-on project to the Uwa Project) to make 95\% + biodegradable drones. It is expected that the Jigu Project will last for a further five years after the Uwa Project has finished. If the Uwa Project is discontinued or sold sooner than four years, the Jigu Project could still be undertaken after four years.

## Uwa Project

The following number of drones are expected to be produced and sold:

| Year | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: |
| Number of drones produced and sold | 4,300 | 19,200 | 35,600 | 25,400 |

In the first year, for each drone, it is expected that the selling price will be $\$ 1,200$ and the variable costs will be $\$ 480$. The total annual direct fixed costs will be $\$ 2,700,000$. After the first year, the selling price is expected to increase by $8 \%$ annually, the variable costs by $4 \%$ annually and the fixed costs by $10 \%$ annually, for the next three years. Training costs are expected to be $200 \%$ of the variable costs in year $1,60 \%$ in year 2 , and $10 \%$ in each of years 3 and 4 . There is substantial uncertainty about the drones produced and sold, and Talam Co estimates the project to have a standard deviation of $30 \%$.

At the start of every year, the Uwa Project will need working capital. In the first year, this will be $20 \%$ of sales revenue. In subsequent years, the project will require additional or a reduction in working capital of $10 \%$ for every $\$ 1$ increase or decrease in sales revenue respectively. The working capital is expected to be fully recovered when the Uwa Project ceases.

The Uwa Project will need $\$ 35,000,000$ of machinery to produce the drones at the start of the project. Tax allowable depreciation is available on the machinery at $15 \%$ per year on a straight-line basis. The machinery is expected to be sold for $\$ 7,000,000$ (post-inflation) at the end of the project. Talam Co makes sufficient profits from its other activities to take advantage of any tax loss relief. Tax is paid in the year it falls due.

## Jigu Project as a real option

Talam Co estimates that Jigu Project's cash flows are highly uncertain and its standard deviation is $50 \%$. It is estimated that $\$ 60,000,000$ will be required at the start of the project in four years' time. Using conventional net present value, Talam Co's best estimate is that net present value of the project will be $\$ 10,000,000$ at the start of the project.
The following figures were estimated for the Jigu Project using the real options method.
Asset value $\left(P_{a}\right)=\$ 46,100,000$ (to nearest 100,000)
Exercise price $\left(P_{e}\right)=\$ 60,000,000$
Exercise date $(t)=4$ years
Risk-free rate $(r)=2 \cdot 30 \%$
Volatility ( s ) $=50 \%$
$d_{1}=0.329 \quad d_{2}=-0.671 \quad N\left(d_{1}\right)=0.6288 \quad N\left(d_{2}\right)=0.2510$
Call option value: $\$ 15,258,399$
It can be assumed that the call option value is accurate.
Talam Co's finance director wants to know how the asset value of $\$ 46,100,000$ has been estimated.

## Honua Co's offer

Honua Co, whose main business is drone production, has approached Talam Co with an offer to buy the Uwa Project in its entirety from Talam Co, for $\$ 30,000,000$ at the start of the third year of the project's life.

Talam Co has calculated some figures to assess the value of Honua Co's offer using the real options method, as follows:
$\mathrm{d}_{1}=0.779$
$d_{2}=0.355$
$N\left(d_{1}\right)=0.7821$
$N\left(d_{2}\right)=0.6387$

Talam Co's finance director has requested that the value of Honua Co's offer is estimated using the real options method. She has also requested to know the amounts of the initial variables which would have been used to calculate the $d_{1}$, $d_{2}, N\left(d_{1}\right)$ and $N\left(d_{2}\right)$ figures.

It can be assumed that the $\mathrm{d}_{1}, \mathrm{~d}_{2}, \mathrm{~N}\left(\mathrm{~d}_{1}\right)$ and $\mathrm{N}\left(\mathrm{d}_{2}\right)$ figures are accurate.
Additional information
Both Honua Co and Talam Co pay corporation tax at an annual rate of 20\%. Talam Co has estimated Uwa Project's and Jigu Project's risk-adjusted cost of capital at $11 \%$, based on Honua Co's asset beta. Talam Co believes that LIBOR, which is currently $2 \cdot 30 \%$, provides a good estimate of the risk-free rate of interest.

## Required:

(a) Discuss how incorporating real options into net present value decisions may help Talam Co with its investment appraisal decisions.
(5 marks)
(b) Prepare a report for the board of directors (BoD) of Talam Co which:
(i) Estimates, showing all relevant calculations, the net present value of the Uwa Project before considering the offer from Honua Co and the Jigu Project;
(12 marks)
(ii) Addresses the requests made by the finance director about the initial variables and estimated value of the offer from Honua Co using the real options method;
(9 marks)
(iii) Assesses whether the Uwa Project should be undertaken, using the results from, and discusses the assumptions made in, the calculations in (b)(i) and (b)(ii) above.
(10 marks)
Professional marks will be awarded in part (b) for the format, structure and presentation of the report.
(4 marks)
(c) At a recent trade show, the biodegradable drones attracted considerable interest from organisations worldwide. Nevertheless, some expressed concern about the drone price, which they felt was too high.

Talam Co estimates that even a modest reduction in each drone's price would make the projects unprofitable. Therefore, the operations director suggested that costs could be reduced if drone components were produced in Dunia, a country where Talam Co already gets some of its other products made.

However, the public relations director brought up an issue concerning Dunia. He said that several companies in Dunia, which Talam Co trades with, employ young teenage children. These companies pay the education fees for the teenagers and the companies argued that stopping this practice would harm the teenagers' families financially.

## Required:

Discuss the impact on Talam Co and its aims arising from the possible sustainability and ethical issues above, and advise on how these issues may be addressed.

## Section B - BOTH questions are compulsory and MUST be attempted

2 Lurgshall Co is a listed electronics company. Lurgshall Co has recently appointed a new chief executive, who has a number of plans to expand the company. The chief executive also plans to look carefully at the costs of all departments in Lurgshall Co's head office, including the centralised treasury department.

The first major investment which the chief executive will oversee is an investment in facilities to produce applications-specific components. To finance the planned investment, it is likely that Lurgshall Co will have to borrow money. It is now 1 May. At present, it seems that Lurgshall Co will need to borrow $\$ 84$ million on 1 September, for a period of six months, though both the amount and the period of borrowing are subject to some uncertainty. The treasurer plans to borrow the funds at a variable rate of LIBOR plus 50 basis points. LIBOR is currently $4 \cdot 5 \%$ but is expected to rise by up to $0.6 \%$ between now and 1 September.

So far, the possibility of hedging a rise in LIBOR of $0.6 \%$ using a forward rate agreement or September \$ futures has been investigated. The results of the calculations for these instruments were as follows:

4-10 Forward rate agreement from Birdam Bank: 5•38\%
Three-month traded September \$ futures: 5•36\%
Lurgshall Co's treasurer also wants to consider using options on futures to hedge loans.
Although Lurgshall Co has not previously used swaps for hedging purposes, the treasurer has asked Birdam Bank to find a counterparty for a potential swap arrangement.

Relevant information about options and swaps is as follows:

## Options

The current price for three-month $\$$ September futures, $\$ 2$ million contract size is 95.05 . The price is quoted in basis points at 100 - annual \% yield.

Options on three-month September \$ futures, \$2 million contract size, option premiums are in annual \%

| September calls | Strike price | September puts |
| :---: | :---: | :---: |
| 0.132 | 95.25 | 0.411 |

It can be assumed that futures and options contracts are settled at the end of each month. Basis can be assumed to diminish to zero at contract maturity at a constant rate, based on monthly time intervals. It can also be assumed that there is no basis risk and there are no margin requirements.

## Swap

Birdam Bank has found a possible counterparty to enter into a swap with Lurgshall Co. The counterparty can borrow at an annual floating rate of LIBOR $+1 \cdot 5 \%$ or a fixed rate of $6 \cdot 1 \%$. Birdam Bank has quoted Lurgshall Co a notional fixed rate of $5.6 \%$ for it to borrow. Birdam Bank would charge a fee of 10 basis points to each party individually to act as the intermediary of the swap. Both parties would share equally the potential gains from the swap contract.

## Treasury staffing

Lurgshall Co's new chief executive has made the following comments: 'I understand that the treasury department has a number of day-to-day responsibilities, including investing surplus funds for the short-term liquidity management and hedging against currency and interest rates. However, these tasks could all be carried out by the junior, less experienced, members of the department. I do not see why the department needs to employ experienced, expensive staff, as it does not contribute to the strategic success of the company.'

## Required:

(a) Compare the results of hedging the $\$ 84$ million, using the options and the swap, with the results already obtained using the forward rate agreement and futures, and comment on the results. Show all relevant calculations, including how the interest rate swap would work.
(b) Discuss the advantages and disadvantages of using swaps as a means of hedging interest rate risk for Lurgshall Co.
(c) Criticise the views of the chief executive about the work carried out by the treasury department and the staff required to do this work.

3 Newimber Co is a listed company which has always manufactured formal clothing for adults and children. It obtained a listing ten years ago after years of steady growth. $70 \%$ of shares in the company are owned by its directors or their relatives, with the remaining $30 \%$ owned by external investors, including institutional investors.

## Sportswear division

Eight years ago it set up a division to manufacture sportswear. This investment has been very successful and the sportswear division now accounts for $40 \%$ of total group revenue, having grown much quicker than the original formal clothing division.

Newimber Co's board has given divisional management at the sportswear division more authority over time, although the board has continued to make major policy and investment decisions relating to the division. Initially, relations between Newimber Co's board and management of the sportswear division were good, but there have been problems over the last couple of years. The sportswear division's management has been frustrated by the board's refusal to approve their recent investment plans on the grounds that they were too risky. In order to achieve operational efficiencies, the sportswear division's management would also like to pursue stricter policies for managing operational staff and suppliers than Newimber Co's board has so far allowed.

In addition, Newimber Co started to prepare an integrated report three years ago, but Newimber Co's board has had difficulties in obtaining all the information it requires for the report from the sportswear division.

## Restructuring

A few months ago, the management of the sportswear division approached Newimber Co's board with a proposal for a management buyout of the sportswear division. However, the price the sportswear division's management was able to offer was insufficient to persuade Newimber Co's board to sell the sportswear division to them.
Newimber Co's board has, subsequently, decided that the sportswear division should be demerged into a new company, Poynins Co. The shareholders and proportion of shares held would be the same for Poynins Co as currently for Newimber Co. The sportswear division's senior management team would become the board of Poynins Co and Poynins Co would seek an immediate listing on the same stock exchange as Newimber Co.

## Financial information

The market capitalisation of Newimber Co's share capital is currently $\$ 585$ million. Newimber Co also currently has $\$ 200$ million $5.9 \%$ loan notes. The loan notes are redeemable in five years' time at a premium of $5 \%$. Newimber Co's equity beta is currently estimated at $1 \cdot 4$. Newimber Co's current cost of equity is $11.8 \%$ and its current before-tax cost of debt is $4 \cdot 5 \%$.

The asset beta of the formal clothing division is estimated to be $1 \cdot 21$. The weighting in estimating Newimber Co's overall asset beta is $60 \%$ for the formal clothing division to $40 \%$ for the sportswear division. The debt beta can be assumed to be zero.

In return for $40 \%$ of the issued share capital of Newimber Co, its current shareholders will receive $100 \%$ of the issued share capital of Poynins Co, corresponding to the assets and liabilities being transferred. The shares in Newimber Co which shareholders have given up will be cancelled. After the demerger, Newimber Co's new market capitalisation can be assumed to be $\$ 351$ million. Poynins Co will have no long-term debt, the liability for the $\$ 200$ million loan notes remaining with Newimber Co.
The current risk-free rate of return is estimated to be $3 \cdot 4 \%$. The market risk premium is estimated to be $6 \%$. A tax rate of $28 \%$ is applicable to all companies.
The sportswear division currently has $\$ 36$ million operating cash flows. Its managers believe that operating cash flows can increase by the following rates once Poynins Co has been listed:

| Year | $\%$ |
| :--- | ---: |
| 1 | 25 |
| 2 | 20 |
| 3 | 15 |
| 4 onwards | 2 |

The sportswear division's managers believe that Poynins Co will require a $\$ 20$ million investment of additional assets in Year 1, rising to $\$ 22$ million in each of Years 2 and 3, and to $\$ 25$ million annually from Year 4 onwards.

## Required:

(a) Discuss the advantages and disadvantages of demerging the sportswear division into a new company.
(b) Calculate:

- The change in the weighted average cost of capital of Newimber Co if the demerger of the sportswear division takes place;
- The valuation of Poynins Co using free cash flows, based on the information and assumptions given and briefly discuss your results.
(15 marks)
(c) Discuss the factors which may determine the policies Poynins Co should adopt for communication of information to its shareholders and other significant stakeholders.


## Formulae

Modigliani and Miller Proposition 2 (with tax)

$$
k_{e}=k_{e}^{i}+(1-T)\left(k_{e}^{i}-k_{d}\right) \frac{V_{d}}{V_{e}}
$$

## The Capital Asset Pricing Model

$$
\mathrm{E}\left(\mathrm{r}_{\mathrm{i}}\right)=\mathrm{R}_{\mathrm{f}}+\beta_{\mathrm{i}}\left(\mathrm{E}\left(\mathrm{r}_{\mathrm{m}}\right)-\mathrm{R}_{\mathrm{f}}\right)
$$

The asset beta formula

$$
\beta_{\mathrm{a}}=\left[\frac{\mathrm{V}_{\mathrm{e}}}{\left(\mathrm{~V}_{\mathrm{e}}+\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})\right)} \beta_{\mathrm{e}}\right]+\left[\frac{\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})}{\left(\mathrm{V}_{\mathrm{e}}+\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})\right)} \beta_{\mathrm{d}}\right]
$$

The Growth Model

$$
P_{o}=\frac{D_{0}(1+g)}{\left(r_{e}-g\right)}
$$

## Gordon's growth approximation

$$
\mathrm{g}=\mathrm{br} \mathrm{r}_{\mathrm{e}}
$$

The weighted average cost of capital

$$
\text { WACC }=\left[\frac{V_{e}}{V_{e}+V_{d}}\right] k_{e}+\left[\frac{V_{d}}{V_{e}+V_{d}}\right] k_{d}(1-T)
$$

## The Fisher formula

$$
(1+i)=(1+r)(1+h)
$$

Purchasing power parity and interest rate parity

$$
S_{1}=S_{0} \times \frac{\left(1+h_{c}\right)}{\left(1+h_{b}\right)} \quad F_{0}=S_{0} \times \frac{\left(1+i_{c}\right)}{\left(1+i_{b}\right)}
$$

Modified Internal Rate of Return

$$
M I R R=\left[\frac{P V_{R}}{P V_{I}}\right]^{\frac{1}{n}}\left(1+r_{e}\right)-1
$$

The Black-Scholes option pricing model

$$
c=P_{a} N\left(d_{1}\right)-P_{e} N\left(d_{2}\right) e^{-r t}
$$

Where:

$$
\begin{aligned}
& d_{1}=\frac{\ln \left(P_{a} / P_{e}\right)+\left(r+0.5 s^{2}\right) t}{s \sqrt{t}} \\
& d_{2}=d_{1}-s \sqrt{t}
\end{aligned}
$$

The Put Call Parity relationship

$$
p=c-P_{a}+P_{e} e^{-r t}
$$

## Present Value Table

Present value of 1 i.e. $(1+r)^{-n}$
Where $r=$ discount rate
$\mathrm{n}=$ number of periods until payment
Discount rate (r)
Periods

| (n) | $1 \%$ | $2 \%$ | $3 \%$ | $4 \%$ | $5 \%$ | $6 \%$ | $7 \%$ | $8 \%$ | $9 \%$ | $10 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 0.980 | 0.961 | 0.943 | 0.925 | 0.907 | 0.890 | 0.873 | 0.857 | 0.842 | 0.826 | 2 |
| 3 | 0.971 | 0.942 | 0.915 | 0.889 | 0.864 | 0.840 | 0.816 | 0.794 | 0.772 | 0.751 | 3 |
| 4 | 0.961 | 0.924 | 0.888 | 0.855 | 0.823 | 0.792 | 0.763 | 0.735 | 0.708 | 0.683 | 4 |
| 5 | 0.951 | 0.906 | 0.863 | 0.822 | 0.784 | 0.747 | 0.713 | 0.681 | 0.650 | 0.621 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.942 | 0.888 | 0.837 | 0.790 | 0.746 | 0.705 | 0.666 | 0.630 | 0.596 | 0.564 | 6 |
| 7 | 0.933 | 0.871 | 0.813 | 0.760 | 0.711 | 0.665 | 0.623 | 0.583 | 0.547 | 0.513 | 7 |
| 8 | 0.923 | 0.853 | 0.789 | 0.731 | 0.677 | 0.627 | 0.582 | 0.540 | 0.502 | 0.467 | 8 |
| 9 | 0.914 | 0.837 | 0.766 | 0.703 | 0.645 | 0.592 | 0.544 | 0.500 | 0.460 | 0.424 | 9 |
| 10 | 0.905 | 0.820 | 0.744 | 0.676 | 0.614 | 0.558 | 0.508 | 0.463 | 0.422 | 0.386 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.896 | 0.804 | 0.722 | 0.650 | 0.585 | 0.527 | 0.475 | 0.429 | 0.388 | 0.350 | 11 |
| 12 | 0.887 | 0.788 | 0.701 | 0.625 | 0.557 | 0.497 | 0.444 | 0.397 | 0.356 | 0.319 | 12 |
| 13 | 0.879 | 0.773 | 0.681 | 0.601 | 0.530 | 0.469 | 0.415 | 0.368 | 0.326 | 0.290 | 13 |
| 14 | 0.870 | 0.758 | 0.661 | 0.577 | 0.505 | 0.442 | 0.388 | 0.340 | 0.299 | 0.263 | 14 |
| 15 | 0.861 | 0.743 | 0.642 | 0.555 | 0.481 | 0.417 | 0.362 | 0.315 | 0.275 | 0.239 | 15 |


| (n) | $11 \%$ | $12 \%$ | $13 \%$ | $14 \%$ | $15 \%$ | $16 \%$ | $17 \%$ | $18 \%$ | $19 \%$ | $20 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 0.812 | 0.797 | 0.783 | 0.769 | 0.756 | 0.743 | 0.731 | 0.718 | 0.706 | 0.694 | 2 |
| 3 | 0.731 | 0.712 | 0.693 | 0.675 | 0.658 | 0.641 | 0.624 | 0.609 | 0.593 | 0.579 | 3 |
| 4 | 0.659 | 0.636 | 0.613 | 0.592 | 0.572 | 0.552 | 0.534 | 0.516 | 0.499 | 0.482 | 4 |
| 5 | 0.593 | 0.567 | 0.543 | 0.519 | 0.497 | 0.476 | 0.456 | 0.437 | 0.419 | 0.402 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.535 | 0.507 | 0.480 | 0.456 | 0.432 | 0.410 | 0.390 | 0.370 | 0.352 | 0.335 | 6 |
| 7 | 0.482 | 0.452 | 0.425 | 0.400 | 0.376 | 0.354 | 0.333 | 0.314 | 0.296 | 0.279 | 7 |
| 8 | 0.434 | 0.404 | 0.376 | 0.351 | 0.327 | 0.305 | 0.285 | 0.266 | 0.249 | 0.233 | 8 |
| 9 | 0.391 | 0.361 | 0.333 | 0.308 | 0.284 | 0.263 | 0.243 | 0.225 | 0.209 | 0.194 | 9 |
| 10 | 0.352 | 0.322 | 0.295 | 0.270 | 0.247 | 0.227 | 0.208 | 0.191 | 0.176 | 0.162 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.317 | 0.287 | 0.261 | 0.237 | 0.215 | 0.195 | 0.178 | 0.162 | 0.148 | 0.135 | 11 |
| 12 | 0.286 | 0.257 | 0.231 | 0.208 | 0.187 | 0.168 | 0.152 | 0.137 | 0.124 | 0.112 | 12 |
| 13 | 0.258 | 0.229 | 0.204 | 0.182 | 0.163 | 0.145 | 0.130 | 0.116 | 0.104 | 0.093 | 13 |
| 14 | 0.232 | 0.205 | 0.181 | 0.160 | 0.141 | 0.125 | 0.111 | 0.099 | 0.088 | 0.078 | 14 |
| 15 | 0.209 | 0.183 | 0.160 | 0.140 | 0.123 | 0.108 | 0.095 | 0.084 | 0.074 | 0.065 | 15 |

Present value of an annuity of 1 i.e. $\frac{1-(1+r)^{-n}}{r}$

| Where | $r=$ discount rate |
| :--- | :--- |
|  | $n=$ number of periods |

Discount rate (r)
Periods

| ( n ) | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 1.970 | 1.942 | 1.913 | 1.886 | 1.859 | 1.833 | 1.808 | 1.783 | 1.759 | 1.736 | 2 |
| 3 | $2 \cdot 941$ | $2 \cdot 884$ | $2 \cdot 829$ | $2 \cdot 775$ | $2 \cdot 723$ | $2 \cdot 673$ | $2 \cdot 624$ | $2 \cdot 577$ | 2.531 | $2 \cdot 487$ | 3 |
| 4 | 3.902 | 3.808 | 3.717 | 3.630 | 3.546 | 3.465 | $3 \cdot 387$ | $3 \cdot 312$ | 3.240 | $3 \cdot 170$ | 4 |
| 5 | 4.853 | $4 \cdot 713$ | 4.580 | 4.452 | $4 \cdot 329$ | $4 \cdot 212$ | $4 \cdot 100$ | 3.993 | 3.890 | $3 \cdot 791$ | 5 |
| 6 | $5 \cdot 795$ | $5 \cdot 601$ | $5 \cdot 417$ | $5 \cdot 242$ | 5.076 | $4 \cdot 917$ | $4 \cdot 767$ | $4 \cdot 623$ | $4 \cdot 486$ | 4.355 | 6 |
| 7 | 6.728 | 6.472 | 6.230 | 6.002 | 5.786 | $5 \cdot 582$ | $5 \cdot 389$ | $5 \cdot 206$ | 5.033 | $4 \cdot 868$ | 7 |
| 8 | 7.652 | 7.325 | 7.020 | 6.733 | 6.463 | $6 \cdot 210$ | 5.971 | $5 \cdot 747$ | 5.535 | $5 \cdot 335$ | 8 |
| 9 | 8.566 | $8 \cdot 162$ | 7.786 | 7.435 | 7.108 | 6.802 | $6 \cdot 515$ | 6.247 | 5.995 | $5 \cdot 759$ | 9 |
| 10 | $9 \cdot 471$ | 8.983 | 8.530 | $8 \cdot 111$ | $7 \cdot 722$ | $7 \cdot 360$ | $7 \cdot 024$ | $6 \cdot 710$ | $6 \cdot 418$ | $6 \cdot 145$ | 10 |
| 11 | $10 \cdot 368$ | 9.787 | 9.253 | 8.760 | $8 \cdot 306$ | 7.887 | $7 \cdot 499$ | $7 \cdot 139$ | 6.805 | 6.495 | 11 |
| 12 | $11 \cdot 255$ | $10 \cdot 575$ | 9.954 | $9 \cdot 385$ | $8 \cdot 863$ | 8.384 | 7.943 | 7.536 | $7 \cdot 161$ | 6.814 | 12 |
| 13 | $12 \cdot 134$ | $11 \cdot 348$ | 10.635 | 9.986 | 9.394 | 8.853 | 8.358 | 7.904 | $7 \cdot 487$ | $7 \cdot 103$ | 13 |
| 14 | 13.004 | $12 \cdot 106$ | 11.296 | $10 \cdot 563$ | $9 \cdot 899$ | 9.295 | $8 \cdot 745$ | 8.244 | 7.786 | $7 \cdot 367$ | 14 |
| 15 | $13 \cdot 865$ | $12 \cdot 849$ | 11.938 | $11 \cdot 118$ | $10 \cdot 380$ | $9 \cdot 712$ | $9 \cdot 108$ | 8.559 | 8.061 | $7 \cdot 606$ | 15 |
| ( n ) | 11\% | 12\% | 13\% | 14\% | 15\% | 16\% | 17\% | 18\% | 19\% | 20\% |  |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | $0 \cdot 862$ | $0 \cdot 855$ | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 1.713 | 1.690 | 1.668 | 1.647 | 1.626 | 1.605 | 1.585 | 1.566 | 1.547 | 1.528 | 2 |
| 3 | $2 \cdot 444$ | $2 \cdot 402$ | $2 \cdot 361$ | $2 \cdot 322$ | $2 \cdot 283$ | $2 \cdot 246$ | $2 \cdot 210$ | $2 \cdot 174$ | $2 \cdot 140$ | $2 \cdot 106$ | 3 |
| 4 | $3 \cdot 102$ | 3.037 | 2.974 | 2.914 | $2 \cdot 855$ | $2 \cdot 798$ | $2 \cdot 743$ | $2 \cdot 690$ | 2.639 | 2.589 | 4 |
| 5 | 3.696 | 3.605 | 3.517 | 3.433 | 3.352 | $3 \cdot 274$ | $3 \cdot 199$ | $3 \cdot 127$ | 3.058 | 2.991 | 5 |
| 6 | 4.231 | 4.111 | 3.998 | 3.889 | $3 \cdot 784$ | 3.685 | 3.589 | 3.498 | 3.410 | $3 \cdot 326$ | 6 |
| 7 | $4 \cdot 712$ | 4.564 | 4.423 | $4 \cdot 288$ | 4.160 | 4.039 | 3.922 | 3.812 | 3.706 | 3.605 | 7 |
| 8 | $5 \cdot 146$ | 4.968 | 4.799 | 4.639 | 4.487 | 4.344 | $4 \cdot 207$ | 4.078 | 3.954 | 3.837 | 8 |
| 9 | 5.537 | $5 \cdot 328$ | $5 \cdot 132$ | 4.946 | 4.772 | $4 \cdot 607$ | $4 \cdot 451$ | 4.303 | $4 \cdot 163$ | 4.031 | 9 |
| 10 | 5.889 | $5 \cdot 650$ | $5 \cdot 426$ | $5 \cdot 216$ | 5.019 | $4 \cdot 833$ | $4 \cdot 659$ | 4.494 | $4 \cdot 339$ | $4 \cdot 192$ | 10 |
| 11 | $6 \cdot 207$ | 5.938 | $5 \cdot 687$ | $5 \cdot 453$ | 5.234 | 5.029 | $4 \cdot 836$ | $4 \cdot 656$ | $4 \cdot 486$ | 4.327 | 11 |
| 12 | 6.492 | $6 \cdot 194$ | 5.918 | $5 \cdot 660$ | $5 \cdot 421$ | $5 \cdot 197$ | $4 \cdot 988$ | 4.793 | $4 \cdot 611$ | 4.439 | 12 |
| 13 | 6.750 | $6 \cdot 424$ | 6.122 | $5 \cdot 842$ | 5.583 | $5 \cdot 342$ | $5 \cdot 118$ | 4.910 | $4 \cdot 715$ | 4.533 | 13 |
| 14 | 6.982 | 6.628 | $6 \cdot 302$ | 6.002 | $5 \cdot 724$ | $5 \cdot 468$ | $5 \cdot 229$ | 5.008 | 4.802 | 4.611 | 14 |
| 15 | $7 \cdot 191$ | $6 \cdot 811$ | $6 \cdot 462$ | $6 \cdot 142$ | 5.847 | $5 \cdot 575$ | $5 \cdot 324$ | 5.092 | $4 \cdot 876$ | 4.675 | 15 |

Standard normal distribution table

|  | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | $0 \cdot 09$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0 | 0.0000 | 0.0040 | 0.0080 | 0.0120 | 0.0160 | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| $0 \cdot 1$ | 0.0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0753 |
| $0 \cdot 2$ | 0.0793 | 0.0832 | 0.0871 | 0.0910 | 0.0948 | 0.0987 | $0 \cdot 1026$ | $0 \cdot 1064$ | $0 \cdot 1103$ | $0 \cdot 1141$ |
| $0 \cdot 3$ | $0 \cdot 1179$ | $0 \cdot 1217$ | $0 \cdot 1255$ | $0 \cdot 1293$ | $0 \cdot 1331$ | $0 \cdot 1368$ | $0 \cdot 1406$ | 0.1443 | 0.1480 | $0 \cdot 1517$ |
| 0.4 | $0 \cdot 1554$ | $0 \cdot 1591$ | $0 \cdot 1628$ | $0 \cdot 1664$ | $0 \cdot 1700$ | $0 \cdot 1736$ | $0 \cdot 1772$ | $0 \cdot 1808$ | $0 \cdot 1844$ | $0 \cdot 1879$ |
| 0.5 | $0 \cdot 1915$ | 0.1950 | $0 \cdot 1985$ | 0.2019 | 0.2054 | 0.2088 | 0.2123 | 0.2157 | 0.2190 | 0.2224 |
| 0.6 | 0.2257 | 0.2291 | 0.2324 | 0.2357 | 0.2389 | 0.2422 | 0.2454 | 0.2486 | 0.2517 | 0.2549 |
| 0.7 | 0.2580 | 0.2611 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| 0.8 | 0.2881 | 0.2910 | 0.2939 | 0.2967 | 0.2995 | 0.3023 | $0 \cdot 3051$ | 0.3078 | 0.3106 | 0.3133 |
| 0.9 | $0 \cdot 3159$ | 0.3186 | $0 \cdot 3212$ | $0 \cdot 3238$ | $0 \cdot 3264$ | $0 \cdot 3289$ | 0.3315 | 0.3340 | $0 \cdot 3365$ | 0.3389 |
| 1.0 | 0.3413 | 0.3438 | 0.3461 | 0.3485 | $0 \cdot 3508$ | 0.3531 | 0.3554 | 0.3577 | 0.3599 | 0.3621 |
| $1 \cdot 1$ | 0.3643 | 0.3665 | 0.3686 | 0.3708 | 0.3729 | 0.3749 | 0.3770 | 0.3790 | 0.3810 | 0.3830 |
| $1 \cdot 2$ | 0.3849 | 0.3869 | 0.3888 | 0.3907 | 0.3925 | 0.3944 | 0.3962 | 0.3980 | $0 \cdot 3997$ | 0.4015 |
| $1 \cdot 3$ | 0.4032 | 0.4049 | 0.4066 | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| 1.4 | 0.4192 | 0.4207 | $0 \cdot 4222$ | 0.4236 | 0.4251 | 0.4265 | 0.4279 | 0.4292 | 0.4306 | 0.4319 |
| 1.5 | 0.4332 | 0.4345 | 0.4357 | 0.4370 | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| 1.6 | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 | 0.4535 | 0.4545 |
| 1.7 | 0.4554 | 0.4564 | 0.4573 | 0.4582 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| 1.8 | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| 1.9 | 0.4713 | 0.4719 | 0.4726 | 0.4732 | 0.4738 | 0.4744 | 0.4750 | 0.4756 | 0.4761 | 0.4767 |
| 2.0 | 0.4772 | 0.4778 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| $2 \cdot 1$ | 0.4821 | 0.4826 | 0.4830 | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.4850 | 0.4854 | 0.4857 |
| $2 \cdot 2$ | 0.4861 | 0.4864 | 0.4868 | 0.4871 | 0.4875 | 0.4878 | 0.4881 | 0.4884 | 0.4887 | 0.4890 |
| $2 \cdot 3$ | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| 2.4 | 0.4918 | 0.4920 | 0.4922 | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| $2 \cdot 5$ | 0.4938 | 0.4940 | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| $2 \cdot 6$ | 0.4953 | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.4960 | 0.4961 | 0.4962 | 0.4963 | 0.4964 |
| $2 \cdot 7$ | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.4970 | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| 2.8 | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.4980 | 0.4981 |
| $2 \cdot 9$ | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| 3.0 | 0.4987 | 0.4987 | 0.4987 | 0.4988 | 0.4988 | 0.4989 | 0.4989 | 0.4989 | 0.4990 | 0.4990 |

This table can be used to calculate $N(d)$, the cumulative normal distribution functions needed for the Black-Scholes model of option pricing. If $d_{i}>0$, add 0.5 to the relevant number above. If $d_{i}<0$, subtract the relevant number above from 0.5 .

## End of Question Paper

